Lecture note

On

ENGINEERING MECHANICS (Th-4)

2nd Semester (Diploma Course)

(As per the syllabus prepared by the SCTE&VT, Bhubaneswar, Odisha)



IDEAL SCHOOL OF ENGINEERING Retang, Bhubaneswar

FUNDAMENTALS OF ENGINEERING MECHANICS

Definitions of Mechanics -

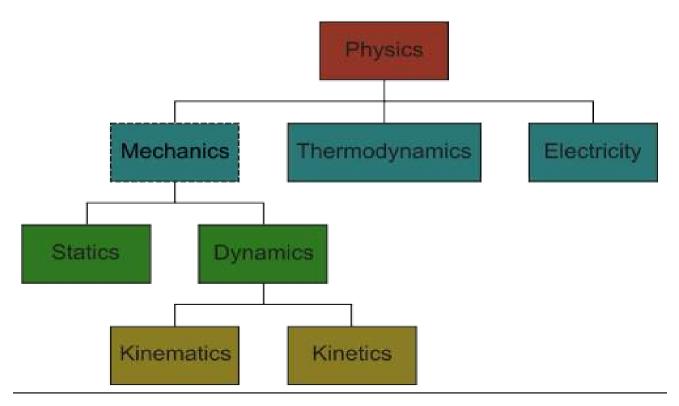
1. A branch of physical science that deals with energy and forces and their effect on bodies.

2. the practical application of **mechanics** to the design, construction, or operation of machines or tools

Definitions of enginnering Mechanics

The subject engineering mechanics is the branch of applied science which deals with the laws and principles of mechanics, along with their applications to engineering problems .

Sub division of Engg. Mechanics



- 1. Particle: A particle is defined as an object that has a mass but no size.
- 2. Body: A body is defined as the matter limited in all directions. It has a finite volume and
- 3. Rigid Body: A body in which the particles do not change their relative positions under the
- action of any external force is called as Rigid Body. No body is perfectly rigid.
- 4. Deformable Body. A body in which the particles change their position under the action of any external force is called as Deformable body.
- 5. Mass: Mass of the body is the quantity of matter contained by the body.
- 6. Weight: The force with which the earth attracts any body to itself is called the weight of the body.



- 7. Space: The unlimited universe in which all the materials are located is known as space. It is a three dimensional region.
- 8. Statics: It is the branch of engineering mechanics which deals with the study of bodies at rest under the action of forces.
- 9. Dynamics: It is the branch of engineering mechanics which deals with the study of bodies
- 10. Kinetics: This branch of dynamics is the study of the behaviour of bodies in motion without considering the forces which causing the motion.
- 11. Kinematics: The kinematics studies the behaviour of bodies in motion by considering the
- 12. Force: It is the agent which changes or tends to change the state of rest or motion of a

Force

Defination –

Force is an external agent capable of changing the state of rest or motion of a particular body. It hasa magnitude and a direction. The direction towards which the force is applied is known as the direction of the force and the application of force is the point where force is applied.

The Force can be measured using a spring balance. The SI unit of force is Newton(N).

Common symbols:	$F \rightarrow, F$
SI unit:	Newton
In SI base units:	kg·m/s ²

Other units:	dyne, poundal, pound-force, kip, kilo pond
Derivations from other quantities:	$\mathbf{F} = \mathbf{m} \mathbf{a}$
Dimension:	LMT ⁻²

Classification of force system according to plane & line of action

System of Forces

When two, or more than two, forces act on a body, they are called to form a system of forces. Following systems of forces are important from the subject point of view :

- 1. Coplaner forces. The forces, whose lines of action lie on the same plane, are known as coplaner forces.
- Collinear forces. The forces, whose lines of action lie on the same line, are known as collinear forces.
- Concurrent forces. The forces, which meet at one point, are known as concurrent forces. The concurrent forces may or may not be collinear.
- Coplaner concurrent forces. The forces, which meet at one point and their lines of action also lie on the same plane, are known as coplaner concurrent forces.
- Coplaner non-concurrent forces. The forces which do not meet at one point, but their lines of action lie on the same plane, are known as coplaner non-concurrent forces.
- Non-coplaner concurrent forces. The forces, which meet at one point, but their lines of action do not lie on the same plane, are known as non-coplaner concurrent forces.
- Non-coplaner non-concurrent forces. The forces, which do not meet at one point and their lines of action do not lie on the same plane, are called non-coplaner non-concurrent forces.

Effects of a Force

A force may produce the following effects in a body, on which it acts :

- 1. It may change the motion of the body, *i.e.* if a body is at rest, the force may set the body in motion, and if the body is already in motion, the force may accelerate it.
- 2. It may retard the motion of a body.
- It may retard the forces, already acting on a body, thus bringing it to rest or in equilibrium. We shall study this effect in chapter 5 of this book.
- It may give rise to the internal stresses in the body, on which it acts. We shall study this effect in chapters 12 and 13 of this book.

Characteristics of a Force

In order to determine the effects of a force, acting on a body, we must know the following characteristics of a force :

- Magnitude of the force (i.e., 10 kgf, 20 tf, 50 N, 15 kN, etc.)
- 2. The direction of the line, along which the force acts (i.e. along OX, OY or at 30° North or East etc.). It is also known as line of action of the force.
- Nature of the force (i.e., whether the force is push or pull). This is denoted by placing an arrow head on the line of action of the force.
- The point at which (or through which) the force acts on the body.

Principle of transmissibility

The state of rest or of motion of a rigid body is unaltered if a force acting on the body is replaced by another force of the same magnitude and direction but acting anywhere on the body along the line of action of the applied forces. In the following animation, two rigid blocks A and B are joined by a rigid rod. If the system is moving on a frictionless surface, the acceleration of the system in both the cases is given

by,

Acceleration=Applied force/total mass

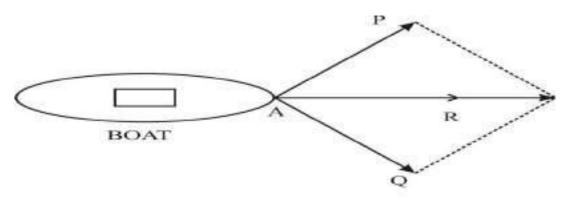
It is independent of the point of application



Principle of Superposition

This principle states that the combined effect of force system acting on a particle or a rigid body is the sum of effects of individual forces.

Consider two forces *P* and *Q* acting at *A* on a boat as shown in Fig.3.1. Let *R* be the resultant of these two forces *P* and *Q*. According to Newton's second law of motion, the boat will move in the direction of resultant force *R* with acceleration proportional to *R*. The same motion can be obtained when *P* and *Q* are applied simultaneously.



Principle of Superposition

Action & Reaction Forces

1. A force is a push or a pull that acts upon an object as a results of its interaction with another object.

2. Forces result from interactions but some forces result from contact interactions (normal, frictional, tensional, and applied forces are examples of contact forces) and other forces are the result of action-at-a-distance interactions (gravitational, electrical, and magnetic forces). According to Newton, whenever objects A and B interact with each other, they exert forces upon each other. When you sit in your chair, your body exerts a downward force on the chair and the chair exerts an upward force on your body. There are two forces resulting from this interaction - a force on the chair and a force on your body. These two forces are called action and reaction forces and are the subject of Newton's third law of motion. Formally stated, Newton's third law is:

For every action, there is an equal and opposite reaction.

The statement means that in every interaction, there is a pair of forces acting on the two interacting objects. The size of the forces on the first object <u>equals</u> the size of the force on the second object. The direction of the force on the first object is <u>opposite</u> to the direction of the force on the second object. Forces <u>always</u> come in pairs - equal and opposite action-reaction force pairs.

Concept of Free Body Diagram

Free-body Diagrams. To investigate the equilibrium of a constrained body, we shall always imagine that we remove the supports and replace them by the *reactions* which they exert on the body. Thus,

3.1. Free Body

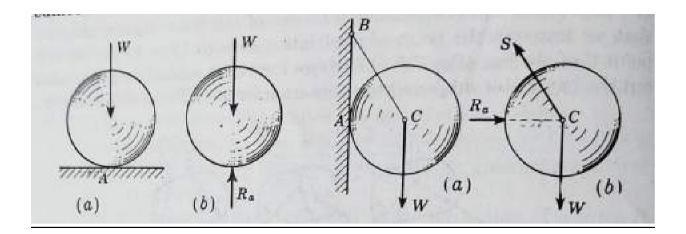
A body is said to be free body if it is isolated from all other connected members,

3.2. Free Body Diagram

Free body diagram of a body is the diagram drawn by showing all the external forces and reactions on the body and by removing the contact surfaces.

Steps to be followed in drawing a free body diagram

- 1. Isolate the body from all other bodies.
- 2. Indicate the external forces on the free body. (The weight of the body should also be included. It should be applied at the centre of gravity of the body.)
- 3. The magnitude and direction of the known external forces should be mentioned.
- 4. The reactions exterted by the supports on the body should be clearly indicated.
- 5. Clearly mark the dimensions in the free body diagram.



Resolution of a Force

The process of splitting up the given force into a number of components, without changing its effect on the body is called resolution of a force. A force is, generally, resolved along two mutually perpendicular directions.

In fact, the resolution of a force is the reverse action of the addition of the component vectors.

2.13. Principle of Resolution

It states, "The algebraic sum of the resolved parts of a number of forces, in a given direction, is equal to the resolved part of their resultant in the same direction."

Proof

Now consider for simplicity, two forces P and Q; which are represented in magnitude and direction by the two adjacent sides OA and OB of a parallelogram OACB as shown in Fig. 2.2.

We know that the resultant (R) of these, two forces Pand Q will be represented, in magnitude and direction, by the diagonal OC of the parallelogram.

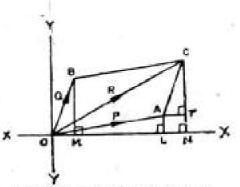


Fig. 2.2 Principle of resolution.

Let OX be the given direction, in which the forces are to be resolved. Now draw AL, BM, and CN perpendiculars from the points A, B and C on OX. Similarly, draw AT perpendicular from the point A on CN.

In the two triangles OBM and ACT, the two sides OB and AC are parallel and equal in magnitude. Moreover, the two sides OM and AT are also parallel.

$$OM = AT = LN$$

Now from the geometry of the figure, we find that

$$ON = OL + LN = OL + OM \dots (\dots LN = OM)$$

But ON is the resolved part of the resultant R, OL is the resolved part of the force P, and OM is the resolved part of the force Q.

Hence resolved part of R along OX

=Resolved part of P along OX

+Resolved part of Q along OX

Note: We have considered, for the sake of simplicity only, the two forces P and Q. But this principle may be extended for any number of forces.

2.14. Method of Resolution for the Resultant Force

The resultant force, of a given system of forces, may be found out by the method of resolution as discussed below :

1. Resolve all the forces vertically and find the algebraic sum of all the vertical components (i.e., ΣV).

2. Resolve all the forces horizontally and find the algebraic sum of all the horizontal components (i.e., ΣH).

3. The resultant R of the given forces will be given by the equation :

$$R = \sqrt{(\Sigma V)^2 + (\Sigma H)^2}$$

4. The resultant force will be inclined at an angle θ , with the horizontal, such that

$$\tan\,\theta\,=\,\frac{\Sigma V}{\Sigma H}$$

Note: The values of the angle θ will vary depending upon the values of ΣV and ΣH as discussed below :

- 1. When ΣV is + ve, the resultant makes an angle between 0° and 180°. But when ΣV is - ve, the resultant makes an angle between 180° and 360°.
- 2. When ΣH is +ve, the resultant makes an angle between 0° and 90° and 270° to 360°. But when ΣH is -ve, the resultant makes an angle between 90° to 270°.

Example 2.3. A triangle ABC has its sides AB = 40 mm along positive x-axis and sides BC = 30 along positive y-axis. Three forces of 40 kgf, 50 kgf and 30 kgf act along the sides AB, BC and CA respectively. Determine the resultant of such a system of forces.

(Osmania University, 1985)

n

Fig. 2-3

50 kg1

30

B

Solution.

The system of the given forces is shown in Fig. 2.3. From the geometry of the figure, we find that the triangle ABCis a right angled triangle in which the *side AC = 50 mm. Moreover.

 $\sin \theta = \frac{30}{50} = 0.6$ $\cos \theta = \frac{40}{50} = 0.8$



Resolving all the forces horizontally (i.e. along AB)

$$\Sigma H = 40 - 30 \cos \theta = 40 - 30 \times 0.8 = 16 \,\mathrm{kef}$$

and now resolving all the forces vertically (i.e. along BC),

$$\Sigma V = 50 - 30 \sin \theta = 50 - 30 \times 0.6 = 32 \, \text{kof} \qquad (ii)$$

We know that the magnitude of the resultant force,

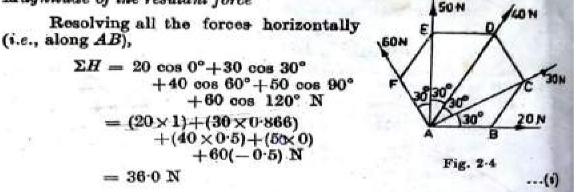
$$R = \sqrt{(\Sigma H)^2 + (\Sigma V)^2} = \sqrt{(16)^2 + (32)^2} \quad \text{kgf}$$

= 35.8 kgf Ans.

Example 2.4. The forces 20 N, 30 N, 40 N, 50 N and 60 N are acting on one of the angular points of a regular hexagon, towards the other five angular points, taken in order. Find the magnitude and direction of the resultant force. (Cambridge University)

Solution.

The system of the given forces is shown in Fig. 2.4. Magnitude of the resulant force



and now resolving the all forces vertically (i.e. at right angles to AB)

 $\Sigma V = 20 \sin 0^{\circ} + 30 \sin 30^{\circ} + 40 \sin 60^{\circ}$ +50 sin 90° + 60 sin 120° N = (20×0) + (30) + (0.5) + (40×0.866) + (50×1) + (60×0.866) N = 151.6 N

We know that magnitude of the resulant force.

$$R = \sqrt{(\Sigma H)^2 + (\Sigma V)^2} = \sqrt{(36 \cdot 0)^2 + (151 \cdot 6)^2} N$$

= 155.8 N Ans.

....(11)

Direction of the resultant force

Let $\theta = Angle$, which the resultant makes with the horizontal (i.e., AB).

$$\frac{\tan \theta}{\Sigma H} = \frac{\Sigma \nu}{\Sigma H} = \frac{151 \cdot 6}{36 \cdot 0} = 4 \cdot 211$$
$$\theta = 76^{\circ} 39' \text{ Ans.}$$

OF

2.

Resultant Force

If a number of forces, P, Q, R, \dots etc. are acting simultaneously on a particle, it is possible to find out a single force which could replace them i.e. which would produce the same effect as produced by all the given forces. This single force is called resultant force, and the given forces P, Q, R, \dots etc. are called component forces.

Composition of Forces

The process of finding out the resultant force of a number of given forces is called *composition of forces* or compounding of forces.

Methods for the Resultant Force

Though there are many methods for finding out the resultant force of a number of given forces, yet the following are important from the subject point of view :

1. Analytical method, 2. Graphical method.

Analytical Method for Resultant Force

The resultant force, of a given system of forces, may be found out analytically by the following methods :

1. Parallelogram law of forces, 2. Method of resolution.

Parallelogram Law of Forces

It states "If two forces, acting simultaneously on a particle, be represented in magnitude and direction by the two adjacent sides of a parallelogram : their resultant may be represented in magnitude and direction by the diagonal of the parallelogram, which passes through their point of intersection." Mathematically, resultant force,

$$R = \sqrt{P^{*} + Q^{*} + 2PQ} \cos \theta$$

and

$$= \frac{Q\sin\theta}{P+Q\cos\theta}$$

where P and Q = Forces whose resultant is required to be found

out,

 θ — Angle between the forces P and Q, and

 α — Angle which the resultant force makes with one of the forces (say P).

oos^a

Note. If the angle (α) which the resultant force makes with the other force Q, then

$$\tan \alpha = \frac{P \sin \theta}{Q + P \cos \theta}$$

tan a =

Cor.

1. If $\theta = 0$ i.e., when the forces act along the same line, then R = P + Q ...(since cos $\theta^{n} = I$)

2. If $\theta = 90^{\circ}$ i.e., when the forces at at right angle, then $R = \sqrt{P^2 + Q^2}$...(since cos $90^{\circ} = 0$)

3. If $\theta = 180^{\circ}$ i.e., when the forces act along the same straight line but in opposite direction then

 $R = P - Q \qquad \dots (since \cos 180^\circ = -1)$ In this case, the resultant force will act in the direction of the greater force.

A. If the two forces are equal i.e. when
$$P = Q$$

4P8 cos2 - 2P cos

then
$$R = \sqrt{P^2 + P^2 + 2P^2 \cos \theta} = \sqrt{2P^2 (1 + \cos \theta)} = \sqrt{2P^2 \times 2 \cos^2 \frac{\theta}{2}} \cdots (\because 1 + \cos \theta = 2)$$

Example 2.1. Two forces act at an angle of 120°. The bigger force is of 40 N and the resultant is perpendicular to the smaller one. Find the smaller force.

Solution Given: P = 40 N; $\angle AOO = 120$; $\angle BOO = 90^{\circ}$ $\therefore \angle AOR$, $\alpha = 120^{\circ} - 90^{\circ}$ $= 3.0^{\circ}$ Let $\cdot Q$ = Smaller force, $Fig. 2\cdot1$ We know that

$$\tan \alpha = \frac{Q \sin \theta}{P + Q \cos \theta}$$

$$\tan 30^{\circ} = \frac{Q \sin 120^{\circ}}{40 + Q \cos 120^{\circ}} = \frac{Q \sin 60^{\circ}}{40 + Q (-\cos 60^{\circ})}$$

$$0.577 = \frac{Q \times 0.866}{40 - Q \times 0.5} = \frac{0.866}{40 - 0.5} \frac{Q}{Q}$$

$$40 - 0.5 Q = \frac{0.866}{0.577} = 1.5 Q$$

$$2Q = 40 \quad \text{or} \quad Q = 20 \text{ N} \text{ Ans.}$$

· Example 2.2. Find the magnitude of the two forces, such that if they act at right angles, their resultant is $\sqrt{10}$ N. But if they act at (Bihar University, 1986) 60°, their resultant is √13 N.

Solution

P and Q = Two given forces. Let

First of all, consider the two forces acting at right angles. We know that when the angle between the two given forces is 90°, then the resultant force (R)

$$\sqrt{10} = \sqrt{P^2 + Q^2}$$

10 = P^2 + Q^2 $\sim \dots$ (Squaring both sides)

Similarly, when the angle between the two forces is 60°, then the resultant force (R)

 $\sqrt{13} = \sqrt{P^2 + Q^2 + 2PQ} \cos 60^\circ$ $13 = P^2 + Q^2 + 2PQ \times 0.5$...,Squaring both sides) ...(Substituting $P^2 + Q^2 = 10$) = 10 + PQPQ = 13 - 10 = 3We know that $(P+Q)^2 = P^2 + Q^2 + 2PQ = 10 + 6 = 16$ $P+Q = \sqrt{16} = 4$(i) 1 $(P-Q)^{2} = P^{2}+Q^{2}-2PQ = 10-6 = 4$ Similarly $P-Q=\sqrt{4}=2$...(ii) 26 Solving equations (i) and (ii). P = 3 N and Q = 1 N Ans.

or

OF:

General Laws for the Resultant Force

The resultant force, of a given system of forces, may also be found out by the following general laws :

1. Triangle law of forces. 2. Polygon law of forces.

Triangle Law of Forces

It states, "If two forces acting simultaneously on a particle, be represented in magnitude and direction by the two sides of a triangle, taken in order-; their resultant may be represented in magnitude and direction by the third side of the triangle, taken in opposite order."

Polygon Law of Forces

Solution.

It is an extension of Triangle Law of Forces for more than two forces, which states, "If a number of forces acting simultaneously on a particle, be represented in magnitude and direction, by the sides of a polygon taken in order; then the resultant of all these forces may be represented, in magnitude and direction, by the closing side of the polygon, taken in opposite order."

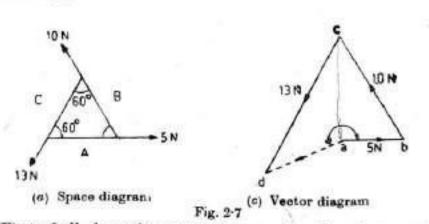
Graphical (Vector) Method for the Resultant Force

This is another name given to the method of finding out, graphically, magnitude and direction of the resultant force by the polygon law of forces. It is done as discussed below :

- Construction of space diagram (position diagram). It means the construction of a diagram showing the various forces (or loads) alongwith their magnitude and lines of action.
- Use of Bow's notations. All the forces in the space diagram are named by using the Bow's notations. It is a convenient method in which every force (or load) is named by two capital letters, placed on its either 'side in the space diagram.
- Construction of vector diagram (force diagram). It means the construction of a diagram starting from a convenient point and then go on adding all the forces vectorially one by one (keeping in view the directions of all the forces) to some suitable scale.

Now the closing side of the polygon, taken in opposite order, will give the magnitude of the resultant force (to the scale) and its direction.

Example 2.7. A particle is acted upon by three forces equal to 5 N, 10 N and 13 N, along the three sides of an equilateral triangle, taken in order. Find graphically the magnitude and direction of the resultant forces. (Madurai University, 1985)



First of all, draw the space diagram for the given system of forces (acting along the sides of an equilateral triangle) and name the forces according to Bow's notations as shown in Fig. 2-7 (a). The 5 N force is named as AB, 10 N force as BC and 13 N force as CD.

Now draw the vector diagram for the given system of forces as shown in Fig. 2.7 (b) and as discussed below :

- 1. Select some suitable point a and draw ab equal to 5 N to some suitable scale and parallel to the force AB of the space diagram.
- 2. Through b, draw bc equal to 10 N to the scale and parallel to the force BC of the space diagram.
- 3. Similarly, through c, draw cd equal to 13 N to the scale and parallel to the force CD of the space diagram.
- 4. Join ad, which gives the magnitude as well as direction of the resultant force.
- 5. By measurement, we find the magnitude of the resultant force is equal to 7 N and acting at an angle of 200° with ab. Ans.

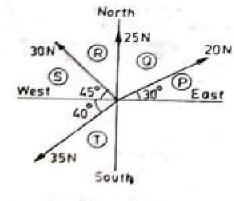
Example 2.8. The following forces act at a point :

(i) 20 N inclined at 30° towards North of East.

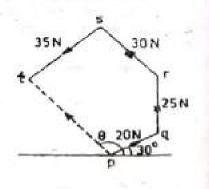
- (ii) 25 N towards North.
- (iii) 30 N towards North West, and
- (iv) 35 N inclined at 40° towards South of West.

Find the magnitude and direction of the resultant force. (Jiwaji University, 1986)

*Solution



(a) Space diagram



(c) Vector diagram

Fig. 2-8

First of all, draw the space diagram for the given ays. In of forces (acting at point O) and name the forces according to Be w's notations as shown in Fig. 2.8 (a). The 20 N force is named as PV, the 25 N force as QR, 30 N force as RS and 35 N force as ST. Now draw the vector diagram for the given system of forces as shown in Fig. 2.8 (b) and as discussed below :

- Select some suitable point p and draw pg equal to 20 N to some suitable scale and parallel to the force PQ.
- Through g, draw gr equal to 25 N to the scale and parallel to the force QR of the space diagram.
- 3. Now through r, draw rs equal to 30 N to the scale and parallel to the force RS of the space diagram.
- Similarly, through s, draw st equal to 35 N to the scale and parallel to the force ST of the space diagram.
- Join pt, which gives the magnitude as well as direction of the resultant force.
- By measurement, we find that the magnitude of the resultant force is equal to 45.6 N and acting at an angle of 132° with the horizontal *i.e.* East-West line. Ans.

2.19. Relation Between Mass and Weight

(The term 'mass' is defined as the matter contained in a body,) whereas the term weight' is defined as the force with which a body is attracted towards the centre of the earth? From the above mentioned two definitions, it is clear that the units of mass are kg, tonnes etc.) whereas the units of weight are N, kN and kgf etc.)

It will be interesting to know that there is an important relation between the mass and weight of a body, which will be discussed in detail in chapter 23 of this book. But for the time being, it may be taken as

$$M P = m q = 9.8 \text{ m}$$

...(g = 9.8)

where

m = Mass of the body in kg, and

 $P \neq \text{Weight of the body in newtons},$

g Gravitational acceleration whose value is taken as 9-8 m/sec².

Example 2.9. A machine shaft BC 1.5 m long and of mass 100 kg is supported by two ropes AB and CD as shown in Fig. 2.9 given below :

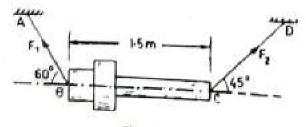


Fig. 2-9

Calculate the tensions F_1 and F_2 in the rope AB and CD.

(London University)

Solution. Given : Mass of shaft = 100 kg

We know that weight of the mass

 $= m.g = 100 \times 9.8 = 980$ N

Resolving the forces horizontally (i.e. along BC) and equating the same,

 $F_1 \cos 60^\circ = F_2 \cos 45^\circ$

:
$$F_1 = \frac{\cos 45^\circ}{\cos 60^\circ} \times F_2 = \frac{0.707}{0.5} \times F_2 = 1.414 F_2 \dots (i)$$

and now resolving the forces vertically,

$$F_{1} \sin 60^{\circ} + F_{2} \sin 45^{\circ} = 980$$

$$(1.414 \ F_{1}) \ 0.866 + F_{2} \times 0.707 = 980$$

$$1.93 \ F_{2} = 980$$

$$\therefore F_{3} = 980/1.93 = 507.8 \ \text{N} \quad \text{Ans.}$$

$$F_{1} = 1.414 \times 507.8 = 718 \ \text{N} \quad \text{Ans.}$$

and

Moment of a Force

It is the turning effect produced by a force, on the body, on which it acts.¹ The moment of a force is equal to the product of the force and the perpendicular distance of the point, about which the moment is required, and the line of action of the force. Mathematically, moment,

$$M = P \times l$$

where

P = Force acting on the body, and

l = Perpendicular distance between the point, about which the moment is required and the line of action of the force.

Graphical Representation of Moment

Consider a force P represented, in magnitude and direction, by the line AB. Let O be a point, about which the moment of this force is required to be found out, as showing the point of the point

From O, draw OC perpendicular to AB. Join OA and OB.

Now moment of the force P about O

 $= P \times O\hat{C} = AB \times OC$

But $AB \times OC$ is equal to twice the area of the triangle ABO.

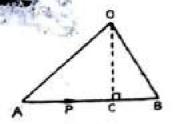


Fig. 3.1

Thus the moment of a force, about Representation of moment any point, is geometrically equal to twice the area of the triangle, whose base is the line representing the force and whose vertex is the point, about which the moment is taken.

Units of Moment

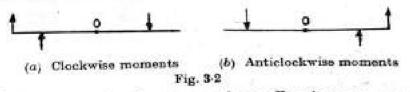
Since the moment, of a force, is the product of force and distance, therefore the units of the moment will depend upon the units of force and distance. Thus, if the force is in Newton and the distance is in metres, therefore the units of moment will be Newtonmetre (briefly written as N-m). Similarly, the units of moment may be kN-m (i.e. $kN \times m$), N-mm (i.e. $N \times mm$) kgf-m (kgf×m) etc

Types of Moments

Broadly speaking, the moments are of the following two types :

1. Clockwise moments, 2. Anticlockwise moments.

Clockwise Moment



It is the moment of a force, whose effect is to turn or rotate the body, in the same direction in which the hands of a clock move, as shown in Fig. 3.2 (a).

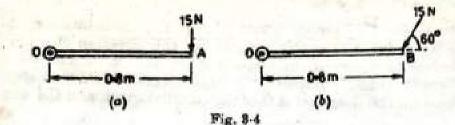
Anticlockwise Moment

It is the moment of a force, whose effect is to turn or rotate the bady, in the *opposite* direction in which the hands of a clock move, as shown in Fig. 3.2 (b).

Note. The general convention is 'J 'take clockwise moment as possitive and appliclockwise moment as negative.

Varignon's Principle of Moments (or Law of Moments)

It states, "If a number of coplanar forces are acting simultaneously on a particle, the algebraic sum of the moments of all the forces about any point is equal to the moment of their resultant force about the same point." **Example 3.1.** A force of 15 N is applied perpendicular to the edge of a door 0.8 m wide as shown in Fig. 3.4 (a). Find the moment of the force about the hinge.



door, as shown in Fig. 3.4 (b), find the moment of this force. (Gujarat University, 1984)

Solution. Given : P = 15 N ; l = 0.8 m

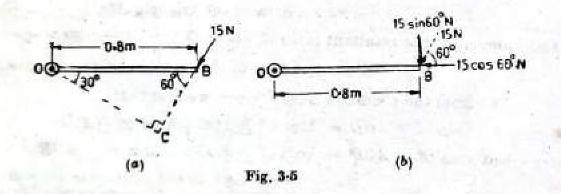
Moment when the force acts perpendicular to the door

We know that the moment of the force about the hinge,

$$= P \times l = 15 \times 0.8 = 12.0$$
 N-m Ans.

Moment when the force acts at an angle of 60° to the door

This part of the example may be solved either by finding out the perpendicular distance between the hinge and the line of action of the force as shown in Fig. 3.5 (a) or by finding out the vertical component of the force as shown in Fig. 3.4 (b).



From the geometry of Fig. 3.5 (a), we find that the perpendicular distance between the line of action of the force and hinge,

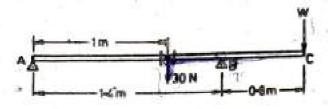
 $OC = OB \sin 60^\circ = 0.8 \times 0.866 = 0.693 \text{ m}$

Moment = 15×0.693 = 10.4 N Ans.

In the second case, we know that the vertical component of the force

. .

 $= 15 \sin 60^{\circ} = 15 \times 0.866 = 13.0 \text{ N}$ Moment $= 13 \times 0.8 = 10.4 \text{ N}$ Ans. **Example 3.2.** A uniform plank ABC of weight 30 N and 2 m long is supported at one end A and at a point B 1.4 m from A as shown in Fig. 3.6.



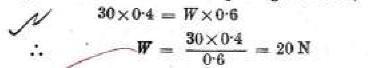


Find the maximum weight W, that can be placed at C, so that the plank does not topple. (Patna University, 1986)

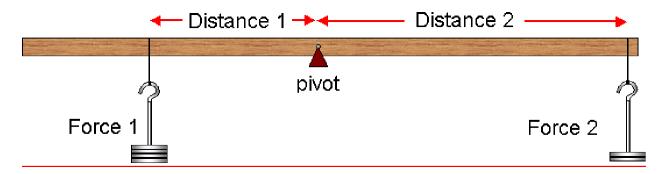
Solution. Given : W = 30 N; Length ABC = 2 m

We know that weight of the plank (30 N) will act at its midpoint, as it is of uniform section. This point is at a distance of 1 m from A or 0.4 m from B.

We also know that if the plank is not to topple, then the reaction at A should be zero for the maximum weight at C. Now taking moments about B and equating the same.



Law of moments



When an object is balanced (in equilibrium) the sum of the clockwise moments is equal to the sum of the anticlockwise moments.

Force 1 x its distance from pivot = Force 2 x distance from the pivot

 $F_1 d_1 = F_2 d_2$

COUPLE

Definition – Couple, in mechanics, pair of equal parallel forces that are opposite in direction. The only effect of a couple is to produce or prevent the turning of a body.

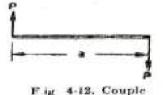
- The turning effect, or moment, of a couple is measured by the product of the magnitude of either force and the perpendicular distance between the action lines of the forces.

Arm of a Couple

The perpendicular distance (a), between the lines of action of the two equal and opposite parallel forces, is known as arm of the couple as shown in Fig. 4.12.

Moment of a Couple

The moment of a couple is the product of the force (*i.e.* one of the forces of the two equal and opposite parallel forces) and the arm of the couple. Mathematically :



Moment of a couple $-P \times p_{-}$

where

$$\mathbf{P} = \mathbf{Force}, \mathbf{and}$$

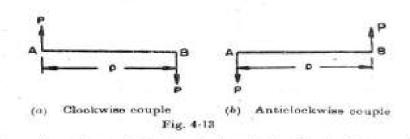
a = Arm of the couple.

Classification of Couples

The couples may be, broadly, classified into the following two categories, depending upon their direction, in which the couple tends to rotate the body, on which they act :

1. Clockwise couple, and 2. Anticlockwise couple.

Clockwise Couple



A couple, whose tendency is to rotate the body, on which it acts, in a clockwise direction, is known as a clockwise couple as shown in Fig. 4.13 (a). Such a couple is also called *positive* couple.

Anticlockwise Couple

A couple, whose tendency is to rotate the body, on which itacts, in an *anticlockwise direction*, is known as an anticlockwise couple as shown in Fig. 4.13 (b). Such a couple is also called a *negative* couple.

Characteristics of a Couple

A couple (whether clockwise or anticlockwise) has the following characteristics :

 The algebraic sum of the forces, constituting the couple, in zero.

- 2. The algebraic sum of the moments of the forces, constituting the couple, about any point is the same, and equal to the moment of the couple itself.
- 3. A couple cannot be balanced by a single force, but can be balanced only by a couple ; but of opposite sense.
- 4. Any number of coplaner couples can be reduced to a single couple, whose magnitude will be equal to the algebraic sum of the moments of all the couples.

Example 46. A square ABCD has forces acting along its sides as shown in Fig. 4.14. Find the values of P and Q, if the system reduces to a couple. Also find magnitude of the couple, if the side of the square is 1 m. (Allahabad University, 1985)

Solution. Given : Length of square = 1 m

Values of P and Q

We know that if the system reduces to a couple, the resultant force in horizontal and vertical directions is zero. Therefore resolving the forces provide the forces of the system reduces to a couple, the resulhorizontally.

 $100 - 100 \cos 45^{\circ} - P = 0$

 $P = 100 - 100 \cos 45^{\circ} N$ = 100 - 100 × 0.70 N = 29.3 N Ans.

Now resolving the forces vertically,

 $200-100 \sin 45^{\circ}-Q = 0$

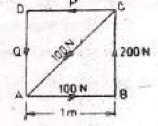
 $Q = 200 - 100 \times 0.707 = 129.3$ N Ans.

Magnitude of the Couple

We know that moment of the couple is equal to the algebraic sum of the moments about any corner. Therefore moment of the couple (taking moments about A)

 $= (-200 \times 1) + (-P \times 1) = -200 - 29.3 \times 1$ N-m

= -229 3 N-m Ans.(Minus sign due to anticlockwise)





CHAPTER-02 EQUILIBRIUM OFFORCES

of a system of forces acting simulteneously on 2.1 a body produces no change in the state of rest on the state of motion of the body, the system of forces is said to be in equilm.

A system of forces an be in equil " under two situations.

13# of the resultant of a number of forces arting at a peint is xerco.

Ly when the nexultant of a system of forces applied on a particle has a non-zero value, then the particle will reamain at rest by applying a force equal in magnitude but opposite in direit of the resultant.

Principles of Equilibrium

Tue - force principle

When a booky is orched upon by tuco, equal opposite collinearic forces, the norultant force is zuco. The eyston of forces is easil to be in equilibrium.

Three non-parallel forces will be in equile" when Three force principle they lie in one plane, intercent of one peint and there free vertons form a closed prisangle.

2.2 Danigs Theoriem of three coplanners concurrent forces are acting on a bedy hapt in equilibrium, then each forces is propertien to the line angle between other tall forces and the const. of propertionality is the same. sing sing - const Pop sinja P. R ! R acting at point 0. het force gince p. q, k are in equilibrium the triangle of forces shell be a closed one. (vertor diagram) Draw as line AB 1 to forcer. Premend A draw a live 11+00. name it Ac. priam's' draw alone 11-to p. 97 well intervient the line AB at B. 2A = T-9 49 = T-B LC ZT-V Applying sine roule to the BABC. Sin(T- on) sin(# -B) sin(T-n) R. Sûn VI sinop sèns

of An electric lamp weighing 201 is superded from apaint a superifed by 2 wine to 2 BC. The point A.B are at same level. Ac makes an angle 60° and BC makes 45° to horizontal as sheren in fig. Determine the tension in the strang AC BC. sol w at c = 20 TAC - tenvior in Ac TBC = " " BC. SON sinar' sinp sinr 20 = TBC - TAC sinth sin 150 Sin 135 . 150 TAC = 20x x0135 = 14.14 = 14.95 AN Sinto $T_{BC} = \frac{a_0 \times sin 3B0}{3in 75} = \frac{10}{3in 75} = \frac{10}{9}$ Sin 75°

(2) Boby weighing 10N is expendended from a foxed paint by astrong 15cm long & is upt at rest by a transfer of force p at a distance of 9 cm from the vertical line draven through the paint of cuspension. What are the trainer of the string & the value of P?

Let terrier T developed in the driving AB. The point B is in equil , moler the three forcies to TAB 2P. 200 let (180 = 0-W= ION Applying Lamile theorem P THE 2 10 sin (90+8) singo sen (180-6)

P = T = 10 COSO = 1 Sine

From DABC

$$ABR' = Ac^{2} + Bc^{2}$$

 $ABR' = AB^{2} - Bc^{2}$
 $= 15^{2} - q^{2}$
 $= 285 - 81$
 $AC = J144$
 $= 120449$

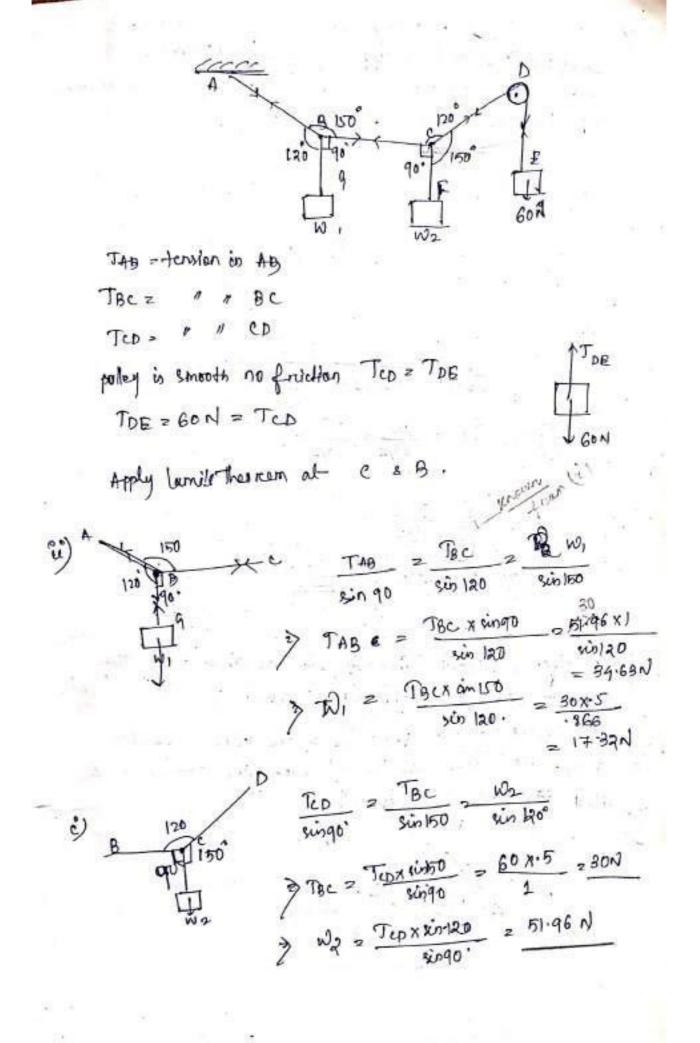
1 2 3

 $8\dot{m}\theta = \frac{\Lambda C}{\Lambda B} = \frac{12}{15} = 2.0.8$ $Cos \theta = \frac{BC}{\Lambda B} = \frac{9}{15} = 2.0.6$ $\frac{1}{1} = \frac{P}{0.6} = \frac{10}{0.8}$ $Cos a = \frac{1}{10}$ $Cos a = \frac{1}{10}$ $Cos a = \frac{1}{10}$ $Cos a = \frac{1}{10}$ $Cos a = \frac{1}{10}$

$$P = \frac{10X0x6}{0x3} = \frac{60}{8} = \frac{10}{5} + \frac{10}{8} + \frac{10}{10} + \frac{10}{10} = \frac{10}{10} + \frac{10}{10}$$

T= 10 = 12.5 A A

2. A fine light string ABCDE with one end A fixed, has necessful wis wis attached to it at B and C. The string passes tround a smooth pulley D carry who what freezeral E as shown infig. If the position of equil, BC is honizental with AB & CD makes an angle 150° & 120° with BC. Ding ii) magnéfuele of W1 2 W2



Twee equal and heavy spheres of 40 mm reading and in equill multipling a cup of reading 120 rom. Show 2 that the rear bets the cup & one sphere is double ap that been the two spheres. As shown in the sin 120 Sip 150 $= \frac{W}{V_3/a} = \frac{P}{V_a}$ R= J2 = 2 P / A > A writeron wheel 600 mm den neeighing 5 km rust agonist a riegid reichargular, black of momm heigh as showen in the fig. Lind the mens of force greep. to turcs the wheel over the covener A & 2016 find scener" on the block, Boomm D= 5W

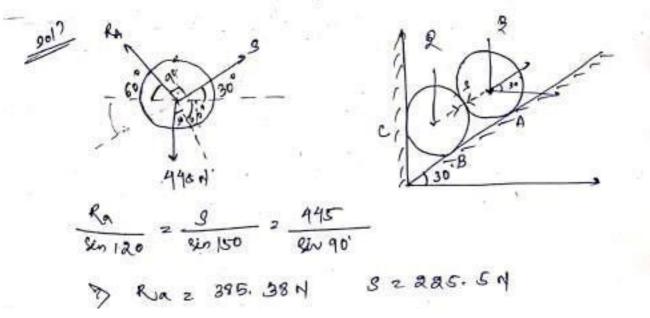
150 120 5 UN 5000 CA singo ° Jun 150 Rin120 4.33 KN P = 1330N 2 2500N 2.5 KA Two spheres with center A& B. Lying is equally, in up with outers of , had the a sphere contact at ptc. and sphere A heith cup @ 2 sphere & with cup E - green at DIE P - ren at c. = 120-40 from geometry. OD = 120 mm AD = 40 mm 50 280. similarly OB= 80. AB = AC+CB 240+40 280 OAB becomes equilateral Δ. R W Zinland Quin R= 13/2 = 1/2 R= 2P

2) A smooth circular cylinder of scordius 1.5 meter & laying en triangular grecove. one side of which makes 15° angle 2 other go angle, with horizental. Find the scenefican at the surface of content. If there is no friction & the cylinder weight 10001. RA: 40 100 N RA - ROOL of A Ro - Real of B RB nin (180-15) sin (15+45 sin(180 - 40) = 78 .54 R3 ~ 31.61 A string. ASCD altached to fired peinds A: D has two equal veeight of 1000N altached to BIC. The weight not with the pontions AB & D inclined angle as shown in fog. 60 100N 1000N Eind the tension in AB, BC & CD

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got free body diagram. 1000-1000 TAB: Win (180-30) sin 150 JAB = 1732 ~ 1000 4 18c = JCD TBC TCD = 1000 N 120 1000 N

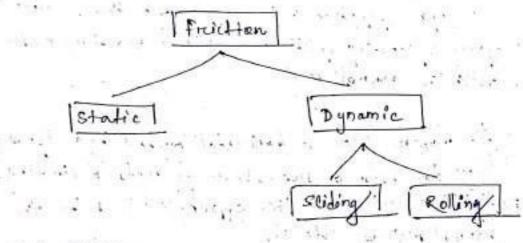
Two identical rollens each of weight &= 945 N are supported by an inclined place and a vertical wall as sheven in the fig. A animing smooth surface, Pind the guerefions induced at pt pt A, B. C



Pp Rb 10 530 Resolving vertically 60 \$7.20 20 Rb cos 30 = 945 + S son 30' 3 69,0003 Rb 2/ Roolning horizontally 2a 20 Rb sin 30" + 5 6330' = Rc Re z Scanned by CamScanner

CHAPTER > 03 FRICTION

3.1 When a bedy Blides on tends to slide even anothere lunface, an apposing force; called as force of friction. It acts targent to the surface and oppositer to the direction the body is moving ex ferrals to more.



Lystatic Prictien

It is experienced by a bidly when it is at rest ore when the body to fendete move.

Leviding Priction It is experienced when a bedy slids once arother bedy.

the second state of the second

See 2 the 1

4 Rolling Priction

It is experiments when a body scalls another another body.

1.462.01.1.1

Lizmiting Freichion

This is the negrimum value of frictional force which comes into play, when a beely) with begins to etide over another bedy, because as limiting friction.

If the applied forces is less than the limiting fristion, the body runains at rust a the fristions is called static fritian, which may have any value bet zero to limiting friction. Angle of freition Engle of friction is the angle which the recouldant of foreve of limiting friction & normal reaction makes with the normal real. - Let mans my kept on horizental. pulled by a force p. when the body is suf about to slide a limiting (P) frittion will act on the apposite ride. R be the normal rear of ust. w. Let oc is the sceneultant bet" R & F., makes an angle of with R. $\triangle OBC$ $+an \phi = \frac{BC}{BO} = \frac{F}{R}$ Coefficient of friction In the realis of friction to the normal scenetion bet a bodies denoted by re " u= F= "fan " > F= UR

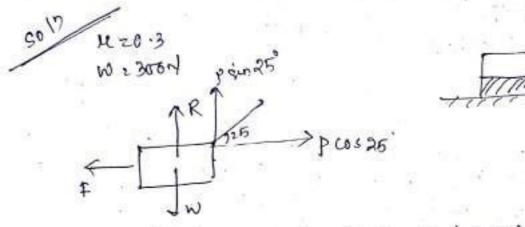
Angle of report

conviden the black of weeight w nuting an an inclined plane which makes an angle a with horizental. When a is very small the block will suf on the plane . of a micrianes gradually ; a stage is reached at which the black will. starts to click . That angle is salled as angle of rapose. waso-W.COS 8 At =0 F= WSm W wind = F. tono = F

ton op = tan 8-> 9-0 Angle of friction = Angle of Repose.

Laws of frostions Ly Laws of static fristion g and he if The force of friction already out opposite on the linee? of applied force. 100 M 41 4 " The magnitude of force of friction is exactly equal to the applied force, , which tend to many . the body . -. The magnitude of the liming friction bears a const ratio to normal reaction bet the free surface. F/R = const. -> The force of friction is independent of the area of contact betn & surface : -> The force of friction depends yoon the surface reoughness. -> Lower of Dynamic friction → the forces of friction always act in a direction opposite in which the bedy is moving. -> For moderates speed the force of friction ecomoins cout, but it decreases with increase of the speed. of a load to Scanned by CamScanner

2) A bedy of veeight 300N is lying on a raugh ponisental plane having a co-efficient of ficiction 0.3. Find the magnitude of the force, which can move the bedy, while acting at an angle of 25° Dith the porizental.

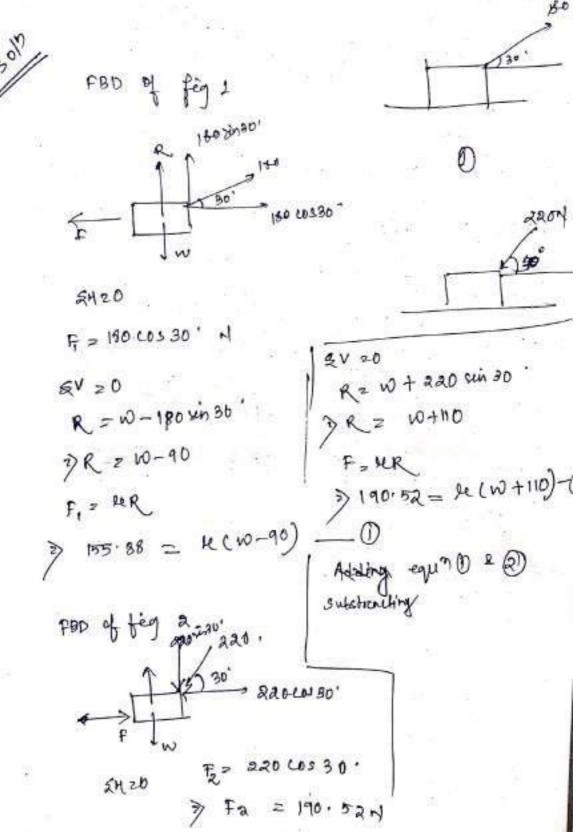


2420 => pcosa5°= F > F= 0.9063p

Neigher
$$= K = 10$$

Neigher $= K = 4R$
 $= 0.9063p = 4 [10 - px.4226]$
 $= 0.9063p = 0.3[300 - .4226]$
 $= 0.9063p = 90 - .1268p$
 $= 0.9063p = 90 - .1268p$
 $= 0.9063p = 87.1 N. Ans$

A body rushing on a neugh horizental plane requer a pull of 1804 molined at 30°, to the plane to to move it st uses found that a push of adon) inclined at 30° to the plane Just m the trady determine the weight of the bedy and the corefficience of friction.

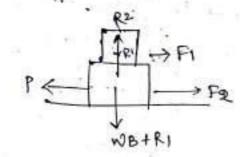


105.88 = WW -904 190.52 = 9LW + 110UL. 6 6 + 34.64 = + 200k > W = 01732 Any ... puting nature of all is equal O We get 155.88 = 0.1732 (W- 90). W = 991.68N 2) if co. efficient - but The & blocks is 0.3. Find force p seen to move the block . WAZ 1KM WB = aKN Trin 30 T KI (verisically) R1 + T sin 30' = 1 km 7/18/18/ TSin 30' 2-2-RI Horizontally TU130°= FI PT COSSO' = FURI > TUBI 30' = 0.3 R, Daviding equation & D $\frac{T \sin 30'}{T \cos 30'} = \frac{1 - R_1}{0.3 R_1} \gg \tan 30' = \frac{1 - R_1}{0.3 R_1}$

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0.5774 = 1-RI 0-3 R1 0.5774×0.3R1= 1-R1 0.173 R,= 1-R1 3 R1 2 0.85 KN 2)

F = AR1 = 0.3 ×0.85 = .255KN



108

 $R_{2} = 2 + R_1$ = 0.85 t = 2.85 KN $F_2 = 9LR_2$

2 0.03 x 2.85 = .855W

= 1.11 KN

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14

A body of net 500 N is lying on a reaugh plane. inclined at an angle of 25°. supported by Aboreizental force pas cheven in feg Defermine p for both upward s downward motion. $p_1 = W \sin(\alpha - \varphi)$ = 16.4 N cos p. Pa = Wsin (n+q) = 376.2 m 6000 2> Andined plane as showen in fig is used to unload abedy of ut 400N. from a height 1.2 m It = 0.3. (State use athere it is necessary to push the body daven the plane are hold it back from "silving dever, what minim force is gueg. parallel for this purpose) And (P) $- \frac{1.8}{2.4} = 0.5$ 5010 1.2m \$, 26.5 400 2 moremal scene? Rz ideoson = 400× 10326.5 = 357.9N FERR A vin or + ALR = P = 400 X 30 265 + 0.3 X 357.9

Equilibrium of a bedy on a rough inclined plane.
Subjected to a force acting horizondally
Consider a bedy lying on a rough inclined plane
subjected to a force acting horizondally.
I Minimum force (P1) which will keep the body in
equil m, when it is at the point of sliding decondered

$$F = 0.8$$
,
 $AH = 0$
 $P \cos n + F = W \sin n$
 $P \cos n = W \sin n - F$
 $P \cos n = W \sin n - KR - O(: F = LR)$
 $SV = 0$
 $R_V = W \cos n + P (inig - 0)$
 $P (\cos n + HP (sin - K in capn 0)$
 $P (\cos n + HP (sin - K in capn 0)$
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In effort of aven is required surf to more certain bedy up an included plane at an angle 15° the focus acting I to plare. If angle spisil " is 20°, then the effect very is found to be abon. Find needyhol of the boly . & in, la = agen) 12 2001 0221 on 2 15° SFA20 FH-WSing = 20 2 2 USA POLR 1+ RODAN IS = 200 > H W LOS or + ala sin 15 2200 > +(+++++++++) = 200 Av 20 RIZW COSM SE4 20 P= WSq120 +F > ur + ws1920 = 230 0 00520 > 91 W LOS 20 +W SIA20 = 230 > M(H LOS 20 + 50 920) 2230 SFr2 0 RR 2 W COSRO selios 20 + SPORO H cos 15 + cin 15 W Q eg O H = 0.25 -> w (-259)x cos 15 + sin-15) 2014 10 N2 392 N

I hand of irren resting on an inclined reargh plane, can be moved up to plane by a face of ann applied horizentally & by a face of 1.25 KN applied 11 to the place. Find engle of inclination s th 6 CO2 01 veost SWCELM pring Q 0 pz w sin(x+q) p= wtan (a t q) 050 25 = 1.5 en(53.1) en(on + q)630 8+9= 63.1 .96 = 620 a = 53.1-16.3 36.8 ye = tan y = tan x 16.3° = .292 R/ Find the force negito more a lead soon upor rough plane the force afting heary " to the place. The inclination of the plane is such that when the same lead is kept on a perfectly emooth plane inclined at angle , of facue 601 applied at an inclination of 30° to the plane, heip the same head in equil19. 12 = 0.3. 407 Rangh. Smooth 1-3 mooth H=0.: \$ 20 30 sings on 210 3 Ces 30" P z w sin (ont P) Ac 0.3 AcRemas 140.74 $hn\phi = 0$ P= 10 sin PE 216.7

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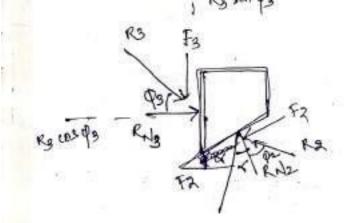
µ= 0.35 Sefercine value of p. 2 ZOON 100 consider the pulley is friction les. Stoint sd 80 FICESO 2000 P = 4 Ro + 800 0032 P = P +800 cos 30' > 5 2000 = Ro + 800 sin30' > Rn = 2000 - 8-10 1430. > putting value of RM. P= 4 × (2000-800 Gin30) + 800 LOS30' = (\$62.52)~ Application of friction LADER PRICTION A balero is a device for climbing on wells. 3.3 - As upper end of the ladder tends to wer slip down ward, freithen (Fw) is upwarco . - As the lenser and trobes to slip away from weall of o ATRY priction (Fy) is towards the weall - Since the system is is equil", thurefore the algebraic sum of heatental & vertical companends of the faced must also be equal to zero.

Muriform hadder of length 3.25m and neighing 250 N placed aganist a smooth vertical reall. 3)'s lower end 1.15 m from the wall. The co-effi viert of friction ber ladder & floor is 0.3. Determine a bread frictional free aling on ladden at paint of contact bet 1 ladder & floor. 00 SV20 & 2 250 N freen geometry BC? = /492- Ac2 125 30m Taking moment about 0. Rfx 1.25 - 250×(1.25) = Ff x3 = 521. N A holder & meter long red on or horizental general and leans against a smooth vertical reall at an angle 70° with harizental. The weight of ladder is good and acts at it's middle. The ladder is at the peint of sliding, when a man weighing 7501 Sards in a the ladder 1.5m from bottom. calulate ef...

55020 60 1: 0m or = 70 50520 WI = good Wa 2 750 N Q= 900 +750 = 1650 N F= 4× Rf 7 Hf × 1650 N_ ~ RA 5 605 70 - 900 x 2.5 (05 70. 1 Wing memery about B +60×3.5 0570 = Ff x.500 70. Rfx15 sindo" = \$ 900 x J.5 eindo -750x 3.5 sindo" = Ffx5 Use" , put the value of Ff Rf x5 sinao - 950 x 2 5 sin 20 - 750 x3 5 sinao = 44 x 650x 5020 (650 × 5 sin 20' 2 (4 f × 1650× 5001 20') + 975 453314 +975 14 = 0.15 AN Two identical blacks of weight ware supported by a need inclined out 45° with horizenfal, as sheven in fig. of both the bleeves are limiting equilibrium, Find the crefficiend of Friction. (has (4). ascuming it to be same as W floor aswellas at wall. Ff

1992 Repulsing forces verdically. FWTRF = 2W _____ New resolving the forces horizotally. Ro = Ft > Ro= HRg-@ Substituting Rul in equit O. 4 (4Rf) +Rf = 2W > H Rf + Rf = 2 W $\geqslant R_{f} = \frac{aW}{(1+H^{2})}$ (3) petting nature of Rf is equ? () $RW = \frac{91}{42} \frac{3W}{42}$ Joking moment of the forces about black A Ruxlies 45° + Fux los 45°= Waltos 43°. RW +FW = W \$ RW + HRW2W PRW (1+4) = W putting value of RN U XAW (1+W)=W 117+1 => &U(HH)= H2+1 2H +242 = H2+) ≥ HR+2H -1=0 l = -3+ (23+9 = 0.414 AS

WEDGE ERICILON A medge is multy, of a triangular is cross-section g is, generally, used for slight adjustments in the position of a body in for tightening fits on keys for shafts of ametimes, a medge is also used for lifting hearry weight. It is made of up revail on metal. Wedge ABC, used to lift the bedy DEFG. N = neight of the body DEFG P = Fonce leag. to lift the body horizonte re = co-efficient of froitiers = tanp novement are get vertical Wwedge - Not considered. lift in upreared When force pirapplied in The body with direction Polz RI-resultant of fruictional fonce & normal scent bet foren enledge. FI ERN e de -> angle of RN2-snownal rece" at AC fraction. & fruidianal force Fa. The next scivillant of both is Rz. onould my an angle \$2. 802



27 A writeron ladders of 4m kength rests against a vertical wall with which it makes an angle. of 95°. The coreffi of freithan bet lodden & wall 04 & that beg? ladder & read floor as. If a man whose weight is one-half of that ladder accessed it. how high itud be when the hadden slips) Fio 50 a, distance bet A & the man neight of man = in = .5W F Ff = Mary = 0.5 Rf FW 2 HWRWZ OGRW RW = R+ = 0.5R+ Ryp = RRW Resolving nontrially RJ+FW = W+ 5.5W > 2RW + 0.9. RW = 1.5W RW = 115W = 0.625W

 $Fw = .4 \times .625W$ = 0.25W Tubing mannert about A. (w x? 0595' + .5W × 2 cos 95) (w x? 0595' + .5W × 2 cos 95) z RW × 4 sin 95 + FW × 604 cos 95

put value of RWS FW

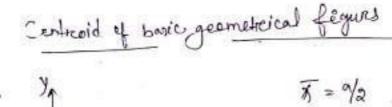
x = 30 3.0 m.

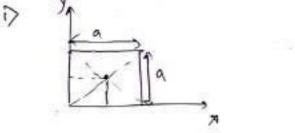
CHAPTER > 04 Centre of Gravety

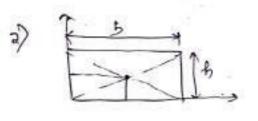
Centre of granity can be defined as a paint through which the whole neight of the body acts, i kneepert of et's position. It may be noted that every body has one and only one contre of granity.

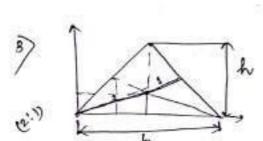
4.1 Centroid

The plane figures like triangle, rectangle, inche et a have only area, but no mars. The centre of arcear of such fig is known as contraid.



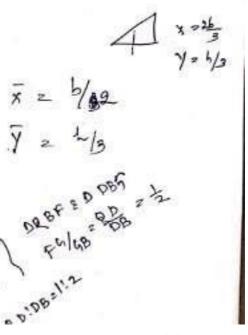




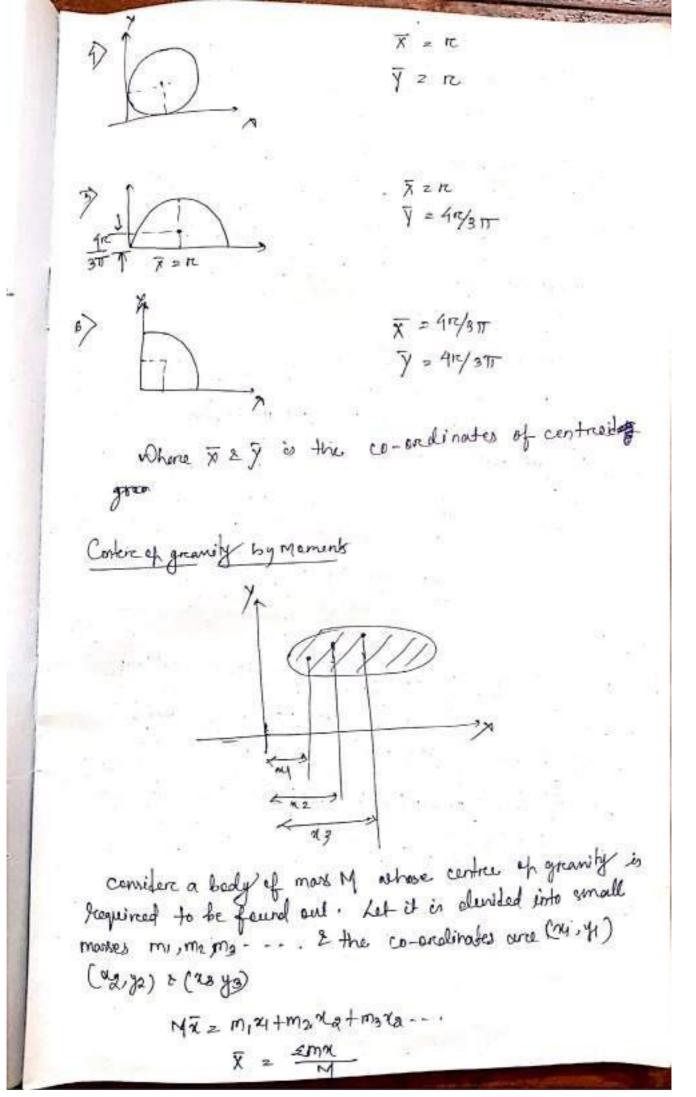




= 9/2



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 $\overline{y} = \frac{x m y}{M}$ $M = m_1 + m_2 + m_3 + \cdots + m_n$

Aris of Reference The centre of gravity of a bedy is alwears calculated with reference to g ome assumed axis alculated with reference, called as axis of Knewer as axis of reference, called as axis of reference. from where F 2 y is calculated.

Centre of granity of plane figure The plane geometrical sections such as J, I, L Sections only have area but no mass. For these the centroid & centre of granity is same.

$$\overline{\mathcal{X}} = \frac{\alpha_1 \alpha_1 + \alpha_2 \alpha_3 + \alpha_3 \alpha_3 + \cdots}{\alpha_1 + \alpha_2 + \alpha_3 + \alpha_3 + \cdots}$$

$$\overline{\mathcal{Y}} = \frac{\alpha_1 y_1 + \alpha_2 y_2 + \alpha_3 y_3 + \cdots}{\alpha_1 + \alpha_2 + \alpha_3 + \cdots}$$

Center of gravity of Symmetrical Sections - If the given section is sympetrical about X-X axis from use have to find X. - If it is symmetrical to Y-Y axis then we have Pofind X & y.

8) true the centre of gravity of 100 non x 1500 m x 300 non of
T. section
9.7 arcs:
10. section of is symmetrical about
y-y arcs:
10. Split the section in & section
ABLD; & PECH
Fore recellingle ABCD:
0.1 = 100 x 30 = 3000 nm²
31 = (150 - 32) = 135 nm
10. ELLargle EEGH
$$a_{x} = 9((50-30) \times 30 = 120 \times 30$$

 $32 = 120/2 = 60 \text{ cm}$.
 $y = \frac{a_{y}(1+a_{x}y_{2})}{a_{1}+a_{2}} = \frac{3050 \times 135 + 3600 \times 60}{9000 + 3600}$
2 94.1mm.
9 (Lettorgle ABSF.
0.1 = 107 x 50 = 750 nm²
 $M_{1} = .50/2 = 25 \text{ mm}$
 $M_{1} = .50/2 = 25 \text{ mm}$
 $M_{2} = 50/2 = 25 \text{ mm}$
 $M_{2} = 50/2 = 25 \text{ mm}$
 $M_{2} = 50/2 = 25 \text{ mm}$
 $M_{3} = 50/2 = 25 \text{ mm}$
 $M_{4} = 50/2 = 25 \text{ mm}$.
3) ectorgle IESH
 $a_{3} = 0000000(000 - 50) 16 \times (100 - 30)$
 $Z = 107 g = 17/g = 7.5 \text{ mm}$

$$\overline{\alpha}_{1} = \frac{\alpha_{1} + \alpha_{2} \alpha_{2} + \alpha_{3} \alpha_{3}}{\alpha_{1} + \alpha_{4} + \alpha_{3}}$$

$$= \frac{1 + \alpha_{4} + \alpha_{3}}{1 + \alpha_{4} + \alpha_{5} +$$

1000

$$\overline{\lambda} = \frac{\alpha_1 \gamma_1 + \alpha_2 \gamma_2}{\alpha_1 + \alpha_2} = 257007$$

$$\overline{J} = \frac{\alpha_1 \gamma_1 + \alpha_2 \gamma_2}{\alpha_1 + \alpha_2} = 357007$$

$$\overline{J} = \frac{\alpha_1 \gamma_1 + \alpha_2 \gamma_2}{\alpha_1 + \alpha_2} = 357007$$

$$\overline{J} = \frac{\alpha_1 \gamma_1 + \alpha_2 \gamma_2}{\alpha_1 + \alpha_2 \gamma_2} = 5000 \text{ mm}^2$$

$$\frac{\gamma_1^{25} + 50}{\alpha_1 = 100 \text{ AFD}} = 50000 \text{ mm}^2$$

$$\frac{\gamma_1^{25} + 50}{\alpha_1 = 100 \text{ AFD}} = 50000 \text{ mm}^2$$

$$\frac{\gamma_1^{25} + 50}{\alpha_2 = 25700}$$

$$\frac{\gamma_1^{25} + 50}{\alpha_1 + \alpha_2 \gamma_2 + \alpha_3 \gamma_3}$$

$$\frac{\gamma_1^{25} + \alpha_2 \gamma_1^{25} + \alpha_3 \gamma_3}{\alpha_1 + \alpha_2 \gamma_1 + \alpha_3 \gamma_3} = 32.2 \text{ mm}$$

55

MOMENT OF INERJIA 4-2 Moment of force = FX I distance. 11st memory of force. of FA Indistance X Ire distance (2nd memerit of focus) are mament smanera M. M. O. F/Brend marmend of of focue) Sometime free & mans can be found out by above metheole. Balso known as Memeril- of merchia. M.M.O.A 1 M.M. D. M Janes Tyy = Eddin (M. I abent = 5 24 . 2.2 Jyy = EdA. x2] - MI abent Lyy z JdA.z? In = [dA.y2] - M.I abent xx aris Moment of inertia = Parevex (porperdicular diston) with = N m2 Moments of inertia of a scelargular. Section considere a reatongalare section b - width sh-the section ABCD . d -> depth of the section Considere a small strip 12 of thickness dy/11 to X-X ats' at a distance of from the centre goes.

Anea of mall strop = dA = bx dy d M.O.I of strip about x- × anis = Area Xya 2 dA. y2 = bxdy. of2 $Tx - X = \int_{-\frac{d}{2}} \frac{dA \cdot q}{\frac{d}{2}}$ = $\int_{0}^{\frac{d}{2}} \frac{dA \cdot q}{\frac{d}{2}}$ 6 3 [(d/2)] <u>_d3/8</u> _ (-d3/8) forhellow Tul 5[7/23 3] $f_{0,y} = \frac{bd^{2}}{12} - \frac{b1d2^{2}}{12}$ db3/12 - di 613/12-Dax = bd3/12. gimilarly Tyy = db3 circular certion M.I ya - Considera exceles ABCD with cuntree 0. consider a reing of radius of and thickness ofte. area épotre rieng d'a = arros. dre MOI about XX onis = direa X distance? anio = atta. da x x2 or xyy = anna dr. Now MIL about the central asis that it be I

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Izz z fina?. da z or Jas don BUDRI The at at]" = Int = I d' (r = d/a) for halles (" In = Iyy= Izc = = Td4 Theorem of perpendicular Anis Dor = Hy 109-d9) = I state that of I've & Igg be the memerit of enertia of a plane section about 2. perpendicula aris metting at 0, The mement of inerifia about Izz about the the aris perependicular to the plane and parsing thriangh intersection of X-X & Y-Y is given by Izz = Ixx + Iyy considercai laminas (p) of , area do having exarchinates a sy an shappanin along ox 2 oy oncis of showener for 1: considerca plane or I tooxe oy. Let re bette distance of Caminar p from 22 ares. op = re from geometry re?= 22+y2-M.I. abent XX Ixx 2 day2 yy Fyyzda. x2.

TAX , da. 12 = da(n²+y²) ~ dane+da.y2 JAZZ INN + IYY

Theorem of parallel ares

If states that. If the M.Z of a plane area about an ancis through it's centre of granity is denoted by IG, then moment of invitin of the areas observe any other areas AB, parallel to the 1st, and Bota distance h from the ciG is given by

IAB = Ig + ah2

IAS -> M.I. of the area about ancis AB

Ig -> M.I - - about cig

a - a near of section

h - distance bet c.g i see" AB

consider a strip of a vincele, where M.I sequined to be found out let Sa = acea if theip y = distance of strip from. A C.G. h sciepnes of C.G. From arcis AB

M.I of while heation about an aris paring through Up = 8a.y?

IG = ESa. y2' MS of whole see paning through CG.

- 52 90

23

 $I_{RC} = \int_{-\infty}^{\infty} \frac{bn}{b} (b-x)^2 dx$ = = fm. (h2+x2-2hx) dx $= \frac{b}{h} \int (mh^2 + m^3 - 2hm^2) dx$ $z = \frac{b}{b} \left[\frac{xR}{a} + \frac{x^9}{4} - \frac{abx^3}{3} \right]^{h}$ $z \frac{b}{h} \left[\frac{h^{4}}{a} + \frac{h^{2}}{4} - \frac{2h^{2}}{a} \right] = \frac{b}{h} \left[\frac{2h^{2} + h^{4}}{24} - \frac{2h^{4}}{3} \right]$ $= \frac{b}{h} \left[\frac{3h^4}{4} - \frac{3h^9}{3} \right] = \frac{b}{h} \left[\frac{9h^4 - 8h^9}{13} \right] = \frac{bh^3}{12}$ M.I. of triangular certion through avis of it's centre of gravity, parallel to X-axis Ig IBC + ad 2 <u>bb</u> bb - <u>bb</u> X(b) d= 1/3 IBC . Ig + ah2 $I_q = \frac{bh3}{36}$ Moment of Inertia of a composite Section Steps

Lo 1st eplit up the given section into plane arens. Lo Dond M.I of these areas about their rupective C.G. Lo Apply parendlel aris theorem. Lo Obtains the M.I.

Cirol 4.2 about axis kk 8 120 > 10 1 0 0 splitup the seen into 0 20 for seen O. IGI = M.I. about c.G about the ancis K-K. $T_{G_1} = \frac{db^3}{12} = \frac{120 \times 40^3}{12} = 640 \times 10^3 \text{ mm}^4$ W1 = 100+40 = 120 mm. C distance bet n c.G of seen O & ancis K-K) M. I of seen are k-k. Ing IGI + aihi -[640x103)+ (120x40)x(120)?] = 69.76×106 mm Similarly M. I of section @ above . it's cog e parcellel to aris Krk. IG2 = db3 = 46.08 × 10 mm 4 ha = 100 + 240 = 220 mm Igz + oz ha? =[46.08×106)+(240×40)×(2008]. = 510.72×10 mm IKK = 69.76×106 + 510.72×106 = 580.48×106 mm 4

2) Find the M.I of a J-section with as 150 mmx.00mm and used 150 mm x50 mm about x-X & y-y axis through the centre of gravity of the section. 15000 301 Reetangle 0 50mm) 0 Q1 = 150 x 50 ≈ 7500 mm2 y1 = 150 + 50 = 175mm 150 000 0 Rechargle 3 Q2 = 150 × 50 = 7500 mm2 \rightarrow 50mm y2 = 150 = 75 mm

 $\overline{y} = \underbrace{a_{4}y_{1}+a_{2}y_{2}}_{a_{4}+a_{2}} \underbrace{(\text{4700 x 175}) + (\text{7500 x 75})}_{a_{4}+a_{2}} \underbrace{(\text{4700 x 175}) + (\text{7500 x 75})}_{a_{4}+a_{2}} \underbrace{\text{4700 + 7500}}_{a_{5}+a$

$$Iq_{2} = \frac{bd^{3}}{1a} = \frac{50 \times (150)^{3}}{1a} + \frac{4.06 \times 10^{6} \text{ mm}^{4}}{1a}$$

$$h_{R} = 125 - \frac{150}{2} = 50 \text{ mm}$$

$$M.J about KX aris IG_{2} + a_{2}h_{2}$$

$$= 14.06 \times 10^{6} + 7500 \times 50^{7}$$

$$= 32.9125 \times 10^{6} \text{ mm}^{4}$$

$$T_{XX} = 20.3125 \times 10^{6} + 32.8425 \times 10^{6}$$

$$= 53.125 \times 10^{6} \text{ mm}^{4} \underline{AM}$$

. .

1G1 = bd3 = 60×203 = 40×108 mm4 WI = 11-7 = 130-60.8 = 69.2mm M:2 of rectangle. O about X-X IGI+ ahi2 = 40×103.+ [1200× (9.2)] = 5786 X10³ Mm 1 $for @ bd^3 = 20x100^3 = 1666.7 \times 10^3 mm^4$ $2Ga^2 = 1a = 12$ ha = ga-y = 70-60.8 = 9.2 mm Tyx22 2 IG2+a2h2 = 1896×103 mm1. for @ IG3 = 100 x203 = 66.7×103mm 4 hs = y-y3 = 60.9-10 = 50.9-mm. JANE 2 IG 3+ aghs = 5228 NOSmmt Dx = \$ (5 + 86 × 10) + (1836×10) + (5 228 × 10) = 12850 ×103 mm4

Find the M.2 about the centreichal . X-X 2 Y-Y axis of the angle section. gol avis. Section is not symmetrical about x ory_ 100 = 100 X Q D = 2000 mm2-Rocelargle () JI = 100/2 = 50 mm 2) az = 80x20 2 16 00 mm2 $y_2 = \frac{20}{2} = 10 \text{ mm}$ $y_{z} = \frac{a_1y_1 + a_2y_2}{a_1 + a_2} = \frac{2000 \times 50}{2000} + 1600 \times 10} = 2.350000$ 2000 + 1600 M. I of O abent X-X axis. $T_{G_1} = \frac{603}{12} = \frac{20 \times 100^3}{12} = 1.667 \times 10^6 mm^4$ tu = y1- y = 50-35 = 15mm Ixa(1) = 261 + 44 h12 = 1-667×10 + 2000×(15)2 2 2.117×18 mm 1 M. I of @ about X-x-axis IGaz baz z 200x 203 = 0.04x 10 mm 4 haz yo- ga = 35-10 = 25mm Inx(2) = IG1 + alh2 = 0.79×108 mm 4

$$T_{X-X} = \frac{D_{X}}{D_{X}} (y) + \frac{D_{X}}{D_{X}} (z) = \frac{3 \cdot 9 \cdot 07}{x 10^{6}} \frac{x 10^{6}}{mm^{4}}$$

$$q_{y} = \frac{2 \cdot 0^{6}}{y} = \frac{10}{mm}$$

$$q_{x} = \frac{2 \cdot 0^{6}}{y} = \frac{10}{mm}$$

$$q_{x} = \frac{2 \cdot 0^{6}}{y} = \frac{10}{2} \frac{2}{2} \frac{2 \cdot 5mm}{m}$$

$$\overline{a} = \frac{a_{1}(x) + 0a_{2}}{a_{1} + 0a_{2}} = \frac{2 \cdot 5mm}{a_{2}}$$

$$q_{1} = \frac{db^{2}}{1a} = \frac{100 \times 20^{3}}{12} = \frac{0 \cdot 06 \times 10^{6}}{mm}$$

$$D_{11} = \frac{db^{2}}{1a} = \frac{100 \times 20^{3}}{12} = \frac{0 \cdot 06 \times 10^{6}}{mm}$$

$$D_{11} = \frac{db^{2}}{1a} = \frac{100 \times 20^{3}}{12} = \frac{0 \cdot 06 \times 10^{6}}{mm}$$

$$D_{11} = \frac{db^{2}}{1a} = \frac{100 \times 20^{3}}{12} = \frac{0 \cdot 06 \times 10^{6}}{mm}$$

$$D_{12} = \overline{a} - x_{1} = \frac{35 - 10}{12} = 1 \cdot 5mm$$

$$D_{12} = \frac{2 \cdot 0.06 \times 10^{6}}{12} + \frac{3000 \times 15^{2}}{12} = 0 \cdot 96 \times 10^{6}} mm^{4}$$

$$D_{12} = \frac{2 \cdot \frac{10^{3}}{12}}{12} - \frac{20 \times 90^{3}}{12} = 0 \cdot 96 \times 10^{6}} mm^{4}$$

$$D_{12} = \frac{2 \cdot \frac{10^{3}}{12}}{12} - \frac{2 \cdot 50 - 25}{12} = 26mm$$

$$D_{12} = \frac{2 \cdot \frac{10^{3}}{12}}{12} - \frac{2 \cdot \frac{10^{3}}{12}}{12} = 1 \cdot 11 \cdot 11 \cdot 10^{6}} mm^{4}$$

$$D_{12} = \frac{1}{2} \cdot \frac{2 \cdot \frac{10^{3}}{12}}{12} = 1 \cdot 11 \cdot 11 \cdot 10^{6}} mm^{4}$$

$$D_{12} = \frac{1}{2} \cdot \frac{2 \cdot \frac{10^{3}}{12}}{12} = 1 \cdot 11 \cdot 11 \cdot 10^{6}} mm^{4}$$

$$D_{12} = \frac{1}{2} \cdot \frac{1}{2$$

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i)

5.1 L'Machino: - 2) is an assembly of interconnected Componente arercarged to pransmit or modify force in ordor to perform weful month.

belies to do some more al some point when effort. Afferce is applied to it.

La compound nachine :- It can be defined as a device which consist of nor of simple machine which enable us to to some weark at a faster speed with loss effort as compare to comple machine.

Lo Lifting Markine : - The nochine which are use to lift heavily lead are called lifting mashine. In a lifting machine a force on lead (w) applied at one point by means of another force called effort (P) applies at another point.

> Mechanical Advantage (M.A) M.A = nlight lead lifted = W offort applied P $M \cdot A = \frac{W}{P}$

2) Velocity Ratio (V.R) V.R. = Wirtance moved by effort = y Distance moved by lead

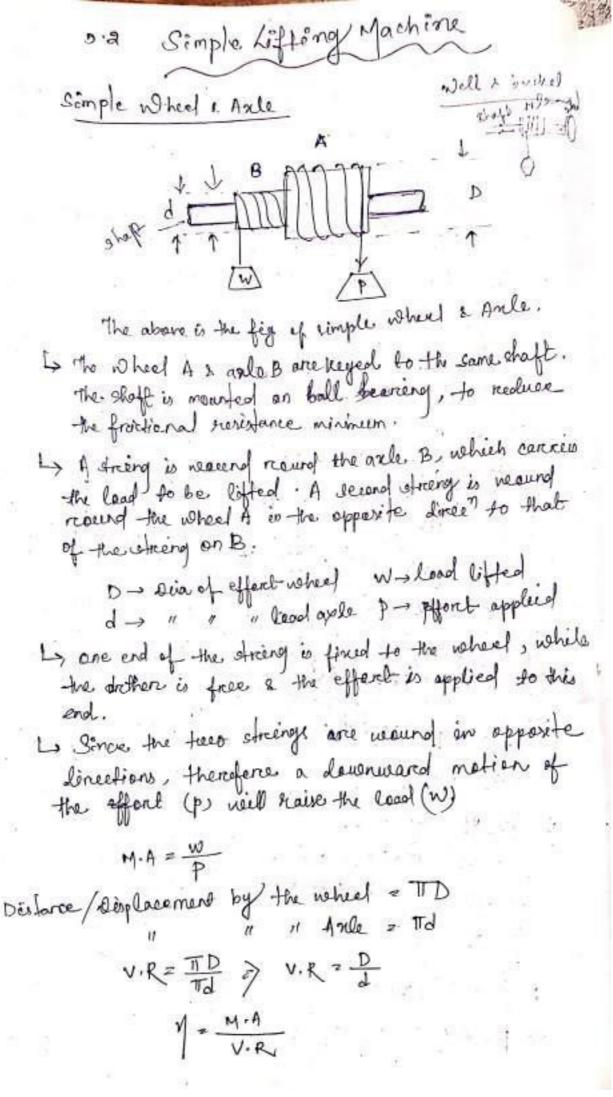
of Input :- it can be defined as workdone on the machine. If is measured by the preschief of effort applied whe distance canned by the effort . i/P = pxy on effort x effort distance. output :- It is defined as the work dance by the machine. . 91 is the preduce of Leod Lifted & Listone renered by the land. Lead x lead sistence . autput = WX2 "efficiency (7) / Relation bet 7 1. M.A. V.R Ratio of where by the machine. Dordy dense on the m/c $= \frac{WXX}{PXY} = \frac{W}{P} \times \frac{2}{8}$ = $\frac{W}{P} \times \frac{1}{9X} = \frac{M \cdot A}{V \cdot R} \times \frac{1}{V \cdot R}$ = $\frac{W}{P} \times \frac{1}{9X} = \frac{M \cdot A}{V \cdot R} \times \frac{1}{V \cdot R}$ Ideal Machine S4 $\int = \frac{M \cdot A}{V \cdot R} = 100 \cdot J$ ie 0/P= i/p. 2) macerifais weight lifting n/e a neight of 1 km islifted by an effort of 25 N. while wit mores by 100mm, the point of application of offerel- moves by 8 m. InLMAINR 19. M == w/P = 40 NR 2 4/K = 80 M=MM/VR = 05 = 50 f. 91) W=1KN p = as N AL= 100 mm = .1 m 8 = 3

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Effect = 50 N (p) Lead (10) = 500 M effort distance = (y) = A5 cm = @ .55m) head distore = (71) = FEM = 0.05M VR = 4/2 = -55 = 1) N.A = 500 = 10 $\gamma = \frac{10}{11} \equiv 0.9.1. = 90.1/.$ 5) v.R = 50 ×leturmin w & p= 60 1 2 70 ℃. VRZ 8/2 1= MA 2 .70 = MA 50 MA = wh 7 MA= 35 > W z 2100 N. Reneresi bility of a Machine. daing Sometimes, a marchine is also capable of daing some nearch in the reversed direction, affer effort is removed. Such a m/c is called a reversible m/c & unover of reversibility of a machine. Candifian for Revensibility of any le N - load lifted by the m/e P - effort seen to lift the load y -> distance moved by effort is slinfance moved by looof.

i/p = pky O/P Z WAX De unew that m/c freition 2 i/p-0/p = pxy - wxx of the m/c is reversible then the o/p of the machine. sherld be more than friction. WHR > PXY-WXX M.A > 12 > anxx > Pxy MA > 50%. MR > 50%. M > 50%. > WXM >12. > w/p > 1/2 So the condition is if the machine is reversible the efficiency is more than 501/ . self locking m/r Some time a machine is not capeble of deing any were wehin the effort is remared. Such machine is called as self locking machine. After the efficiency sheuld not be more than 50.1. Low of Machine. Law of muchine may be defined as the scelationship between effort applied & land lifted. Mathine Heally it is p2 mWtc p- effort w - head lifted Elope)m-> conof confitzent Pomo ideal N/c C - Another Lemit. seeprenut m/c fruition . amount -> load of ficilian need to creacene by the machine.

124 what lead can be lifted by an affent of 12011. if the vele. ratio is 18 2 1/2 60%. Determine the law of the machine, if it is observed that an effort. of about is may to lift a load of 20000 & find the affent seen to run the mile at a lead of 3. MUN. col V.R 2 4/n= 18 Pz/ab 1 2.6 $\frac{w/p}{y_R} = \frac{16}{16} \frac{w}{p} = \frac{18 \times 6}{18 \times 6}$ 2 93 10.9 3 W = 120× 9×19.10.9 = 1296N Lawsof m/c p= 200 W=2600 Pz mw +c 120 = mx 1296 + y - 0 200 = MX2600+ (- 2) +80= + M 1304 7 m= 0.061 put the value of m is equi 2 100= 0.061X-1296+C 200= 0.061X26004C 20015 > C = 44 New effort seen. to suff a loop of 315th > 35×10 1 P = . 061x 3.5×103+44 P=25JN AN



worm & nue D end drum. Lo of convit of a square threaded screw. S (knewer as nearm) & a toothed wheel (known as nearmy nether!) geared to each other .. Ly A wheel A is attached to the acorm, over uchich passes anope as sheven in fig. D- Ding of effort wheel te - redues of the load arean. N- lead P -> Effert applied t → No. of teeth on the worr wheel. M.A = W Displace Distance mored by wheel = TD " " Load drum = ATTZ V.R = TTD = DI = don -if the there is theread of n no. then V.R = DT 1 = M.A V.R

Simple. Screw. Jack It consist of a screw, fitted in a nut, which forms the body of the Jock. The principle, an which a screw wards, is similar to that of an inclied plane. Lo The fig charos a rimple screw Jack . 17 L - leng the of effect and P -> effort-W -> Land p -> pitch of the served the distance moved by the effect in one reevolution - attl Distance moved by the least 2 p V.R = att MA = W Single purchase Creab Monch In a single purchase enablished, a repe is find to the drum e is neound a few turns arround it.

The free end of the rope carries a load w. 1.4 toothed valued 4 is nightly mounted on the lead draws L'Another toothid wheel B called penion is geared with wheel A. Ti - No. of texts in whell/gean A. " / " B. Ta- " " e - langth of handle He - reading of lead drum W -> Level p - efford . Distance moved by the affect in one recolution of hande = attl No. of scevol made by binien B = 1 " A = T2 11 lead drewn = TA/TI listance moved by lead = 21112 xT2/11 VIR= ATTL = TIXL ATTRXTOPI = TAXTL $MA = \frac{W}{P} \int q = \frac{W \cdot A}{V \cdot R}$ Double purchase creat vainely

Э

It is the impressed version of single purchase weak and here there are a spun wheel & 2 pinion.

TI meshed with Ta (pinion) J3, , , J4 (pinion) t = length of the hadke . Tisty = No of teeth in span wheels Tably z " " penson re = radius of drum W. - lead p z peffent Distance maned by effort in one kundlution of bardle = attl r lo. of scenol? made by pinnen 9 - 1 , cour 3 = Ty/T3 " pointing = Ja/T3 11. epun 1 = T2 × 1/9 Distance moved by lead = atax To x To VIR = _ att att (TR/TI) (T3/T4)= + (7/2× T1/T3) M. F= W/P = M.A V.R

CHAPTER-06

DYNAMICS

6.2

Dynamics :- It is the study of motion of regid body and their relation with the forces causing them.

The enline system of dynamics is based on 3 laws of motion. Also known as mareton laws of motion.

~ lenston's 1st law

It states that " Every bedy continues in its state of rest are of uniform motion, in a straight line, when it is acted up on by some assernal force. It also called as have of inertia.

- Lo & bedy at rest has a tendency to reemain at not called inertion of rest.
- Lo A bedy in uniform motion in a streaightline has a tendency to preserve its motion. Known as inertial of motion. A I

Newton's 2nd Law

"The reader of change of momentum is directly propentional to the impressed force and takes place, in the same dire" in which the force acts".

m = mass of a bealy U = gritial velo. of the booky V = Final velo of the bedy a = conf. acc17 to 2 fime. is seconds sug. to change the velo Uto V. F = Forces seen to change velo from wto is at the

Initial mamenbugs mu final = mV Rate of change of momentum = mv-mv = m(v-v) t 2 ma Ace to and land Forma (··· <u>v-v</u>-9) > F= Kma M -> const. For convenience, the will of fance adapted in whether that it produces will all in whit more. F2 ma 2 manix accl In s.I system unit of force is Newton -> N. A Newton may be defined as the force while acting upon a mans of 1 kg, produces an acel of 1 m/sd in the dire" of which it acts. Also knowen as how of dynamics. of all is due to greanity a 29.8 m/s2 = 1 kg. wt Frma (1 kg-wt = 9.8 N) F = 9.8 1000000 N [1. y.F = 9-8N) 2080800 = 1 kg. wb body has song mars on earth. Find a where g=9.84/12 by on moon g=1.7m/s2 ≥u ever. g = 270m/s2 F1 2 50 X 93 Fa 2-50 x 1-7 P3 - 50 12 70

Konetic equations i) v= utat s zub+% al2 3 122UR+ 205 2) + particles of more may share from nost & marger under the influence of a court face. I requires a speed of om/s after 125. > And force on the particle ie) Find speed at 1-2/12 a) First distance covered by the particle is fit , furing time 105. (V) Find interend 5 to 158. m = mans of the particle 250g = 0.05 kg UZO 1 = 6 m/s t = 12, e > v = v + at\$620+ax12 Frma > a'z 6/12 = 0.5 m/s2 : Famxo 2 . 05 X. 0.5 = 0.02 5 N ii) Vzutat = 0 + (0.5 × 16.) = (80 m/s iii) sz vol.+ 1/2 al? 2 0+ + × 0.5×10 - 25m δv $S_{a} - S_{1} = \left(u + \frac{1}{2} a +$

Newton and law for secoil of guin When bullet is fined from agun, the apposite scention of the bullet is known as seeked of que. M -> Mars ef gun. m -> May of Whet. V - velo. of gun v - neb if willet after being fined. memoritum before of the gun = MV , bullef = mV MV = mv Law of conservation of Momentum. Salembert's preinciple A system of forces alting on a body is motion is in dynamic equilib with chentia farce of the body. gnerefia -> Resist motion

-s const + be at oust CFR the resultant of S, Fa, F3 let het a mans m. Fo of we near to bring the boly preduces at rest, nee have to apply a force tooo is opposite dires TR. fiema whose value is equal to ma.

where the jointher force is to bring the body in the first
where no invertion forces to bring the body in the first

$$equal P$$
.
 $FR = 0$
 $FR = ma = 0$
 $Fi \equiv ma$
 $ma = sinvertion force $s = Pi + Also under as curvered
force.
 $Far = 0$
 $Far = 0$
 $From = 1$ force $s = Pi + Also under as a curvered
 $far = 0$
 $From = 1$ for $force = Pi + Also under $force = 0$
 $From = 1$ force $s = 10^{-4}$ force $force = 10^{-4}$ force.
 $W = F \cdot S$
 $From = 1$ force $(S D)$
 $force = 0$
 $From = 1$ force $(S D)$
 $force = 0$
 $From = 1$ force $force = 10^{-4}$ force.
 $From = 1$ force $force = 10^{-4}$ force $force = 10^{-4}$$$$$

Energy I a the capacity to do work. Hereists in many forms , yestanical , electrical Chemical, heat, light etc. unit Came as neorth = Janle - of ycinetic = 1/2 mv3 Mechanical Energy potential = mgh Rinefic Energy energy possed by a bedy, by vintue of its mans & velocity. Energy powed by a bedy, by wetue of its posilion. A truck of mars 15 tonios travelling at 1.6 m/s. Imp neith a spreny Low of concernation of Energy I states that " Chargy on neither be created non destrayed, though it can transformed from one form to another form.

thansformation of brangy . Considere a bedy of mans muchich is released from rest from hight to above the ground. m = manset the body h = height o Grangy at A side at A body has O velocity NE=0 pe = mgh total energy = petke = mgh energy af B . The booky travelled & distance from A to B. 50 · V 2. 1294 He at $B = \frac{mv^3}{2} = \frac{mv^3$ P=E = mg Ch-y) = mgh -mgy total energy = kette = maky + mgh - mgy = mghi thorque at c At a bedy has fallen a hight h. V = V Zgh = mgh $ke = \frac{mva}{a} = \frac{m(2gw)^{3}}{2}$ total energy - ke the - mgh P8 =0

A range bull in prelonged from reader from the top of som high huilding. And -les change in p. 42 35 when it is afor highs of lo from . to great an = 100gm = 0.1kg WI = ROM PEF mgh, - ' 161 = 0 Impulse -> when a const forcer Facts on a body for à lime inferiral. E. Known as groubre. I = FXt and N-S Linearc momenting) Kow it conservation of Linear momentum Ace to newton's and law, the meterician face alting on a body is equal to reale of charge of linear momintum / mancentum. This leads to the law of conservation of lineare memertur for abody which states that the linear momentum of a body leimass const. if the external force on a bedy is Zerco.

5.3 collision of Blastic Bedies

When tues bedies shalles weith each other with actain velocity it is known as callision.

to it (wall or floor) also benever as cellision.

Ly het any ball strikes to the floor, it rises certain height or repoinded.

Lo . This prependy of badius by winter of which , they repounded after imposed is called elasticity.

Lo gut if a body does not exchaund at all, after import called as inelastic collision.

Phenomenon of cellision

- The baddes, immediately after cellision, come memerilarity
- The twee bodies tend to compress each other, so long as they are compressed to the majoin value called as time of compression. (tc)

- The process of regioning of onegenal shape from the deformed shape of the bedies called restitution. Time takes for that called as time of restitution (tr.)

Time of collision = Time of comprovion + Tone of realitudion

haw of concernation of Momentum of states that a the total momentum of two boolies remains conf. after their collision. m101+ mava = m1v1+ m222 m1 = mons of 1st bealy ma = " " and body UI, UR = emitial nelocity of mans mix ma scorpized " mis ma " Virva: final 11 Newtons haw of collicion of elastic bodies I states " when two moving bodies callide with each othere, their velo. of separation hears a const seatio to their rele. of appreach. (V2-V1) = e (U1-V2) where ui-ng e = co-efficient of restitution V1 > va -> collision takes place. Separation talesplace. Va>VI proce Types of collision Direct collision -> Dudicel

Direct cellisions The line of import of the two colliding bedies , is in the line Joining the unters of the 2 bodies, known as peine of contact or paint of collivian. m101+ m202 = m2V1+m2V2. The nature of a is in bet " 0 to 1 if e=0 cillision is inclusfic 2010 222 " elastic. A ball of mass a up mening with a valacity an/see hit another ball of mars of key at read , after imposed We sol ball comes to scort. Cal velo, of the and ball after imposet. & certifi of rescrititution mi = Rug 01 2.2 m/s ma = A way VI = = 0 (cemes densit U2 2 0 at runt (m2) $m_1 v_1 + m_2 v_2 = m_1 v_1 + m_2 v_3$ 2×2 = 4×V2 > Va = 1 m/s (v2-v1) = c. (U1-U2.) e = 1-0 = 1 = 2 0.5 An Theo balls of montres and & 3 kg are moving with 12015 velo am/s 2 3n/s towards each other of e = 0.5. fined prelacity of the tace balls offen collision. 0123 U2 2 9

Scanned by CamScanner

-> U, (2 e - Va-VI m1 A = V2-V1 - V2-V1 2-(-3) -Va. > we vi set toret. 2 = 2 V2-4 > Va+V1 = -5/2 0 > -Va-Vi = 1/2 -> VQ = -5/2 +V1 millitmald z minitmal put the value at > ax2 + 3 (-3) = av1 + (-3 v2) (equ @ -0 2V1-3V2=-5 21-3(-72-1)=5 2) av1+15/2+3V12-5 multiply 2 . 241-342 = -5 ineq (3×2) - 2×1-2×2=+5 > V1 2-255/3 -5V2 = .0 V2 = Om/s Now V1 = - 7/2 = - 2.5 m/s Va = D " A ball is alsopped framial height of Law on a Smooth floor and it rebound be a hight of 570. Depremente the coefficient of estilation between the ball & the floor & also determine the espected beight of the and seabound U - s vele before impored V > r after h - high before " 10m to, - " after 14 seebeerd 5m

11 and

h - 11